

Classification of Edge-dependent Labels of Nodes in Hypergraphs



Minyoung Choe



Sunwoo Kim

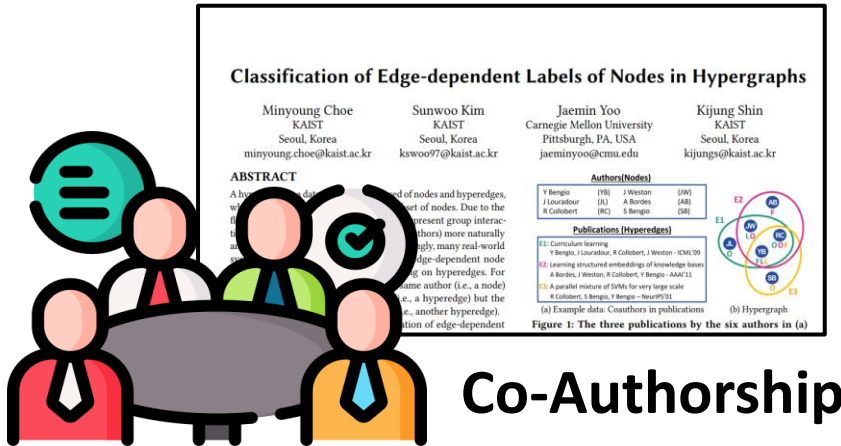


Jaemin Yoo



Kijung Shin

Group Interactions are EVERYWHERE



Co-Authorship

Q&A Platform

How do I set up my local machine with SSO?

Asked by []

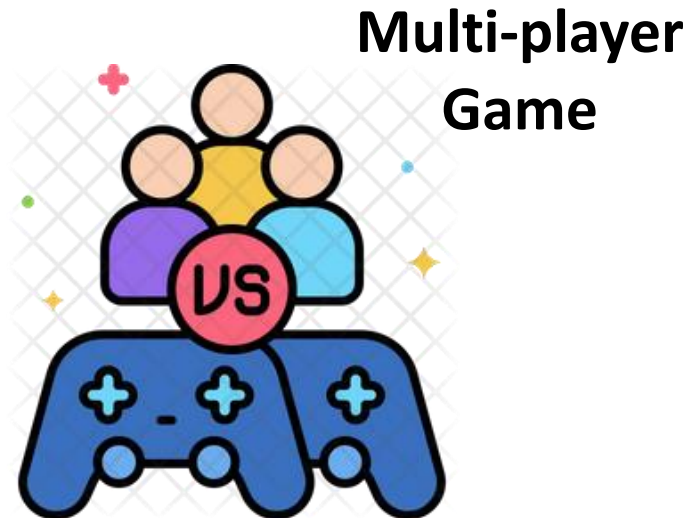
63

✓

Answered by []

2

Answered by []



Email



Group Interactions → Hypergraph

Authors(Nodes)

Y Bengio	(YB)	J Weston	(JW)
J Louradour	(JL)	A Bordes	(AB)
R Collobert	(RC)	S Bengio	(SB)

Publications (Hyperedges)

E1: Curriculum learning

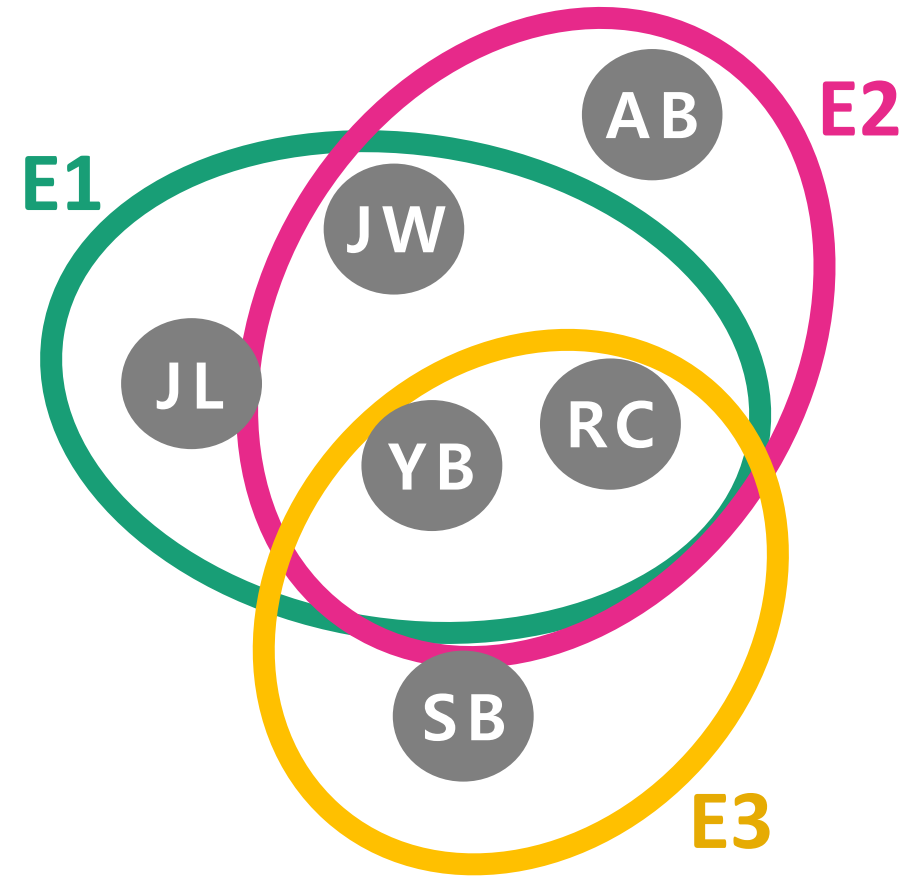
Y Bengio, J Louradour, R Collobert, J Weston - ICML'09

E2: Learning structured embeddings of knowledge bases

A Bordes, J Weston, R Collobert, Y Bengio - AAAI'11

E3: A parallel mixture of SVMs for very large scale

R Collobert, S Bengio, Y Bengio – NIPS'01



Node Labels are Edge-Dependent

Publications (Hyperedges)

E1: Curriculum learning

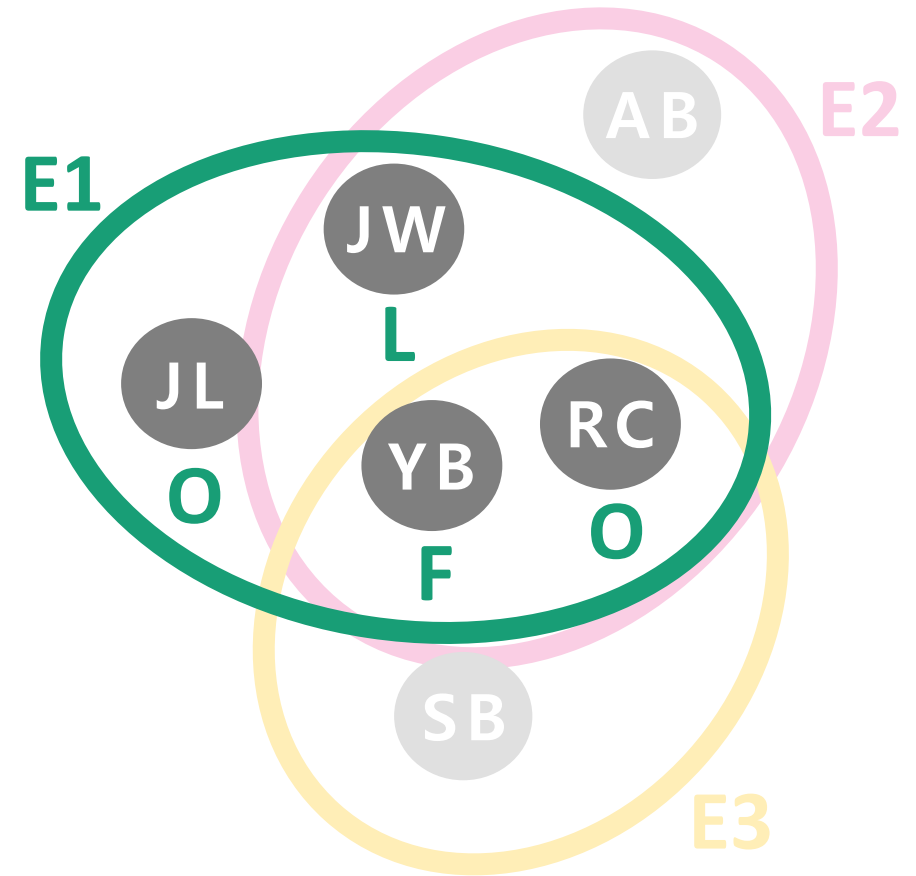
Y Bengio, J Louradour, R Collobert, J Weston - ICML'09

First
(F)

Others
(O)

Last
(L)

**The importance or role of a node
can vary depending on hyperedges!**



Node Labels are Edge-Dependent

Publications (Hyperedges)

E2: Learning structured embeddings of knowledge bases

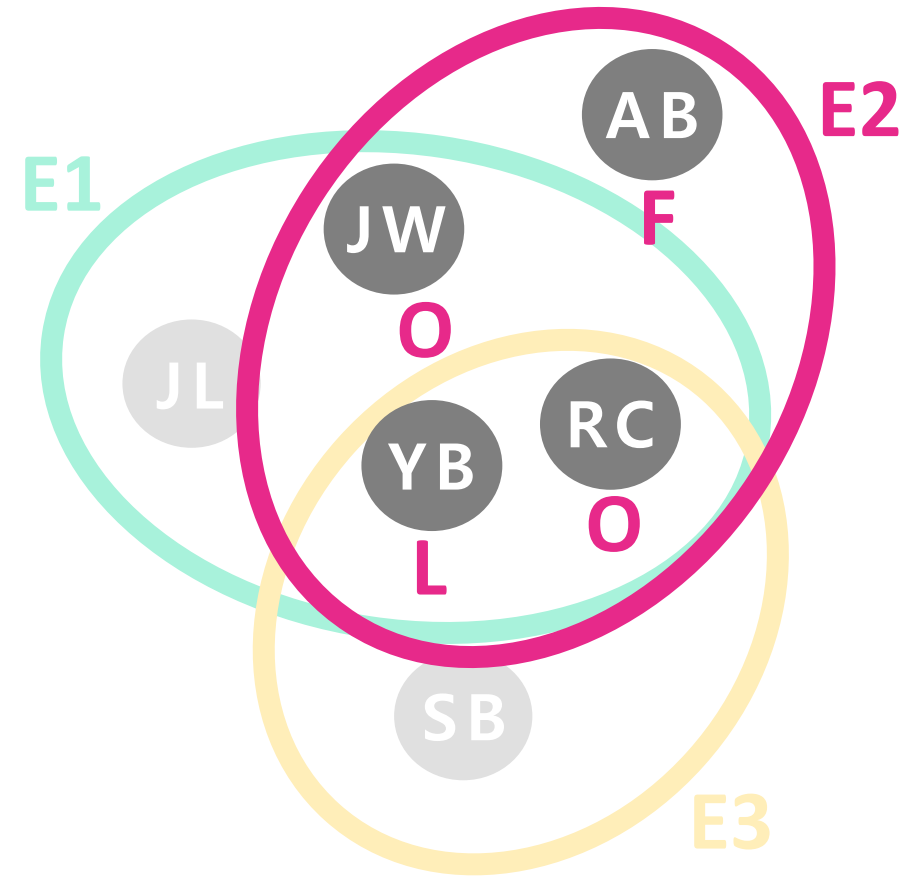
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**The importance or role of a node
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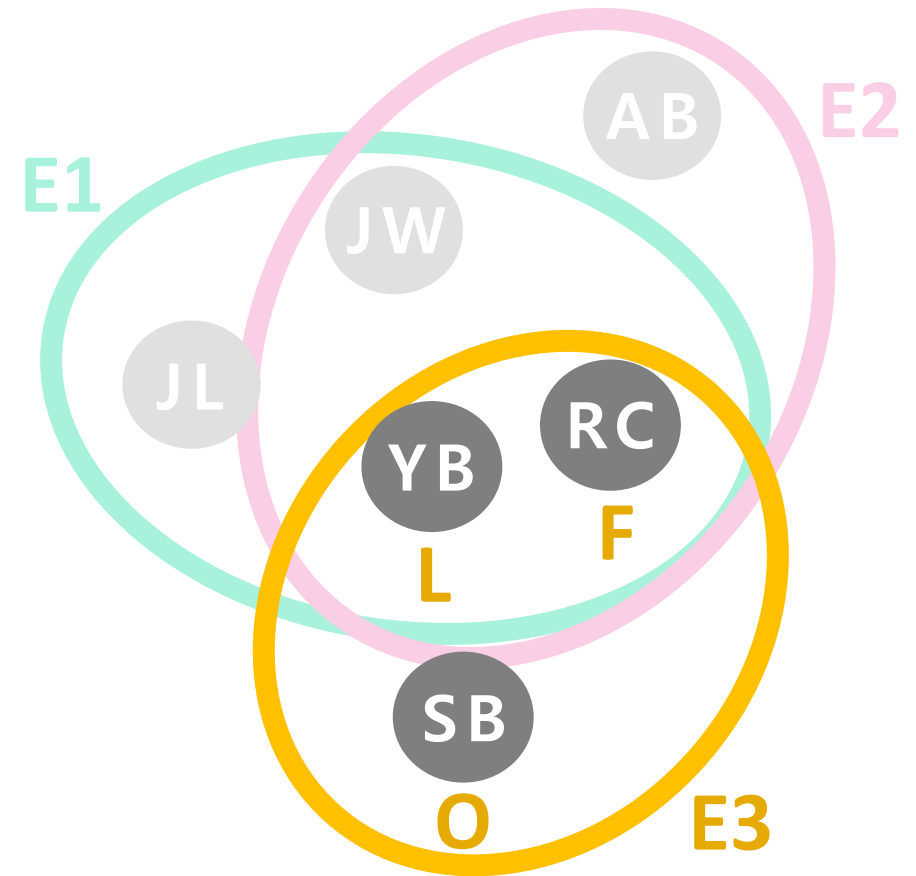
Node Labels are Edge-Dependent

Publications (Hyperedges)

E3: A parallel mixture of SVMs for very large scale
R Collobert, S Bengio, Y Bengio – NIPS'01

First Others Last
(F) (O) (L)

**The importance or role of a node
can vary depending on hyperedges!**



Roadmap

1. Introduction
- 2. Problem Formulation <<**
3. WHATsNET: Proposed Approach
4. Evaluation
5. Conclusions



Problem Formulation

Edge-Dependent Node Classification

- Given**
- A hypergraph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$: a node set \mathcal{V} and a hyperedge set \mathcal{E}
 - A set of edge-dependent node labels in $\mathcal{E}' \subset \mathcal{E}$:

$$y_{v,e}, \forall v \in e, \forall e \in \mathcal{E}'$$

- (Optionally) a node feature matrix X

Aim to *accurately predict* the unknown edge-dependent node labels in $\mathcal{E} \setminus \mathcal{E}'$:

$$y_{v,e}, \forall v \in e, \forall e \in \mathcal{E} \setminus \mathcal{E}'$$

Edge-Dependent Node Classification

Co-Authorship

Publication (Hyperedge E1)

E1: Curriculum learning

Y Bengio, J Louradour, R Collobert, J Weston - ICML'09

Publication (Hyperedge E2)

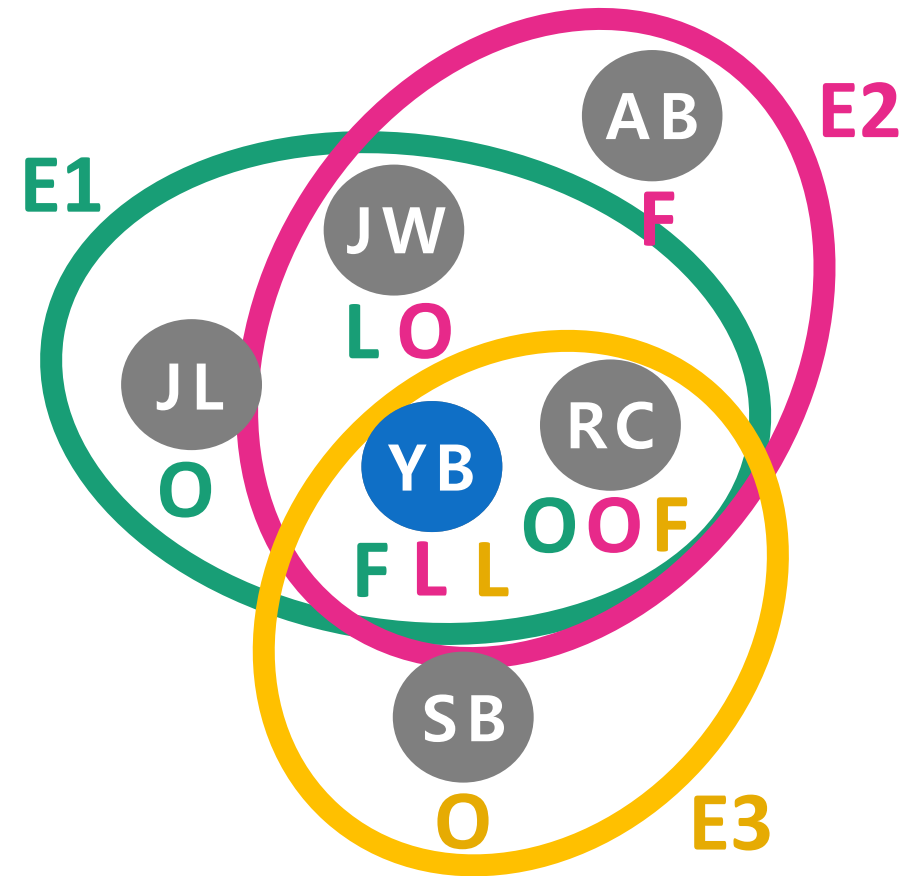
E2: Learning structured embeddings of knowledge bases

A Bordes, J Weston, R Collobert, Y Bengio - AAAI'11

Publication (Hyperedge E3)

E3: A parallel mixture of SVMs for very large scale

R Collobert, S Bengio, Y Bengio – NIPS'01

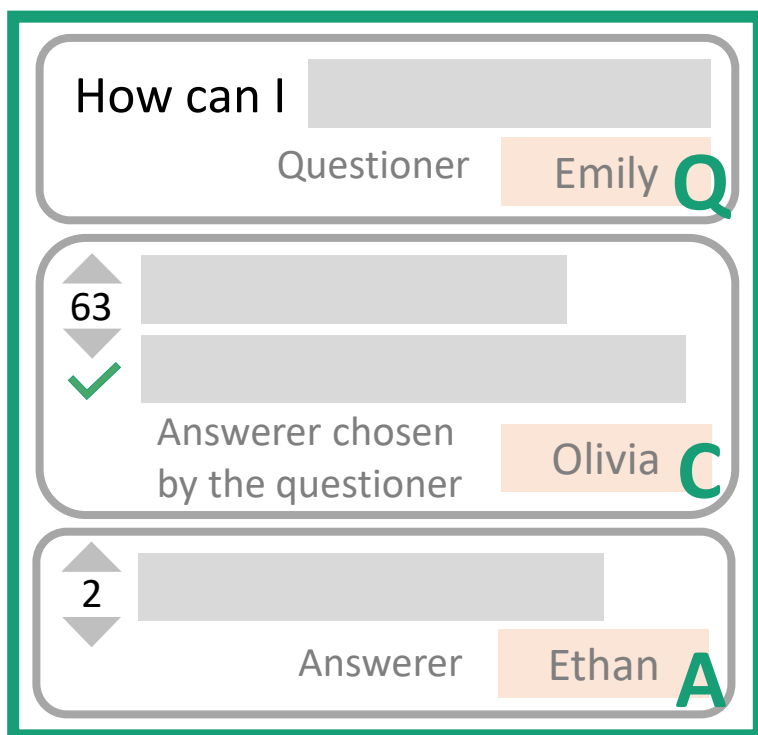


Labels: First, Last, or Others

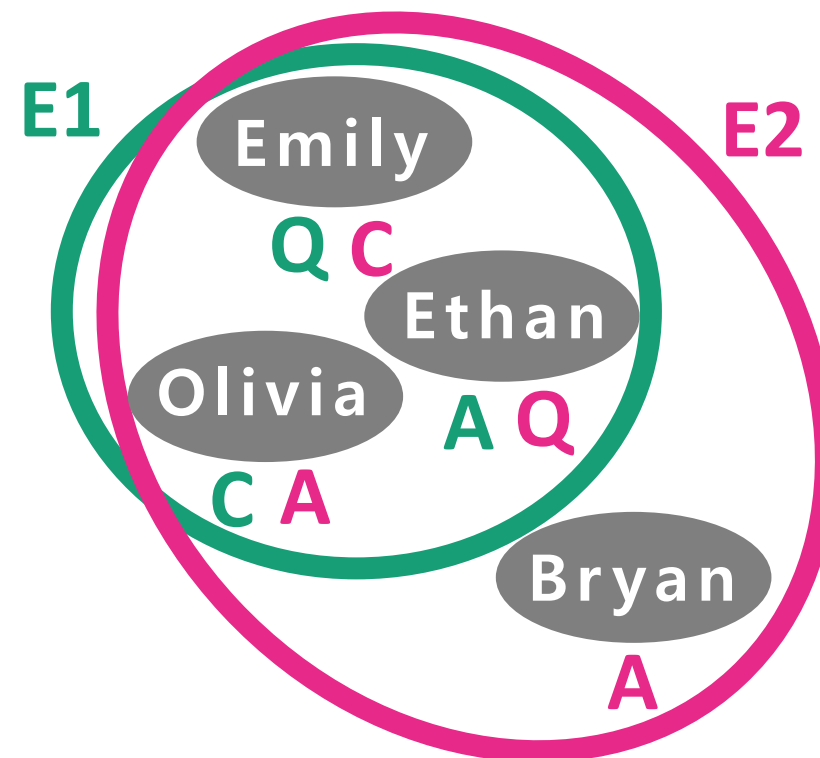
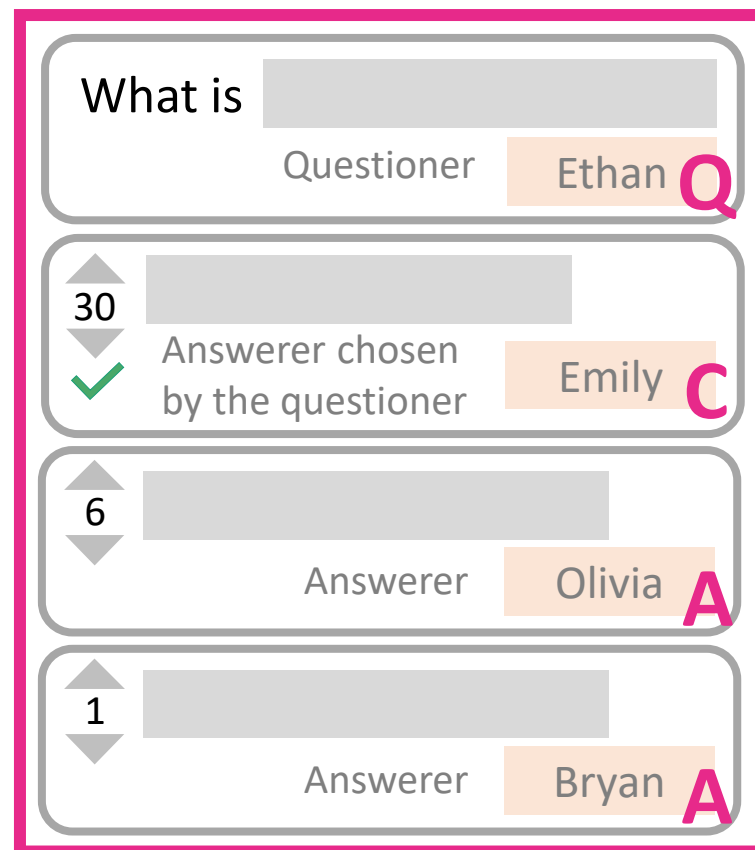
Edge-Dependent Node Classification

Online Q&A Platforms

Post (Hyperedge E1)




Post (Hyperedge E2)




Labels: Questioner, Chosen Answerer, or Answerers

Edge-Dependent Node Classification

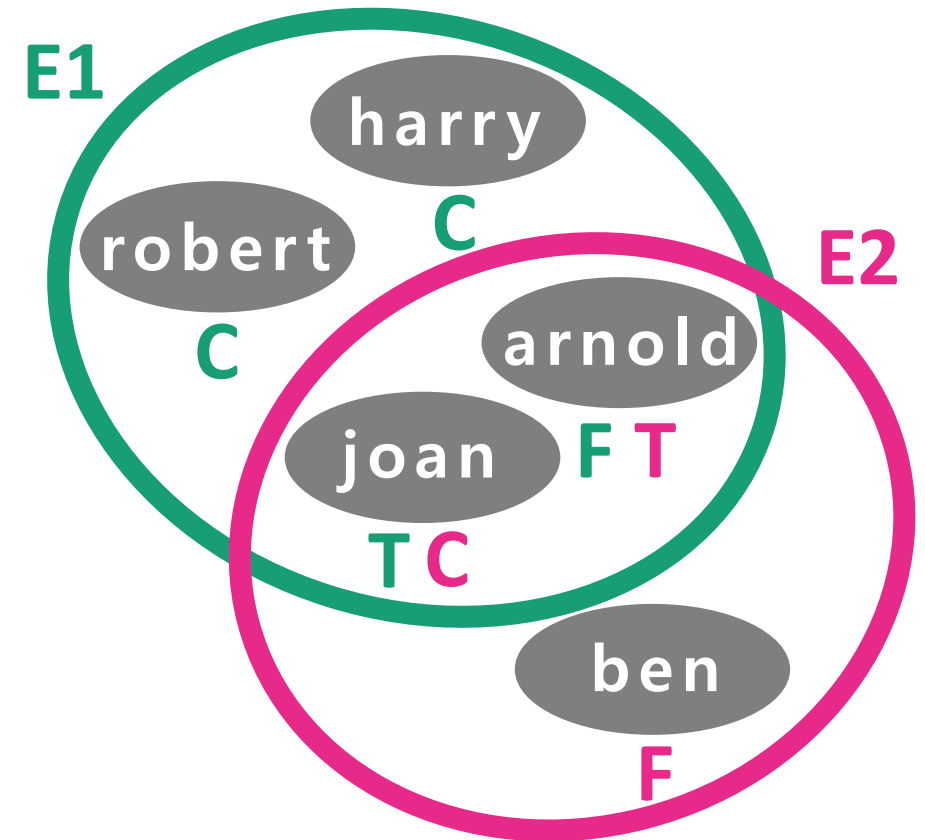
Emails

 **Email (Hyperedge E1)**

To	Joan@enron.com
CC	harry.arora@enron.com, robert.badeer@enron.com
From	arnold@enron.com
TITLE : Today's meeting	

 **Email (Hyperedge E2)**

To	arnold@enron.com
CC	Joan@enron.com
From	ben@enron.com
TITLE : Issue on the project	



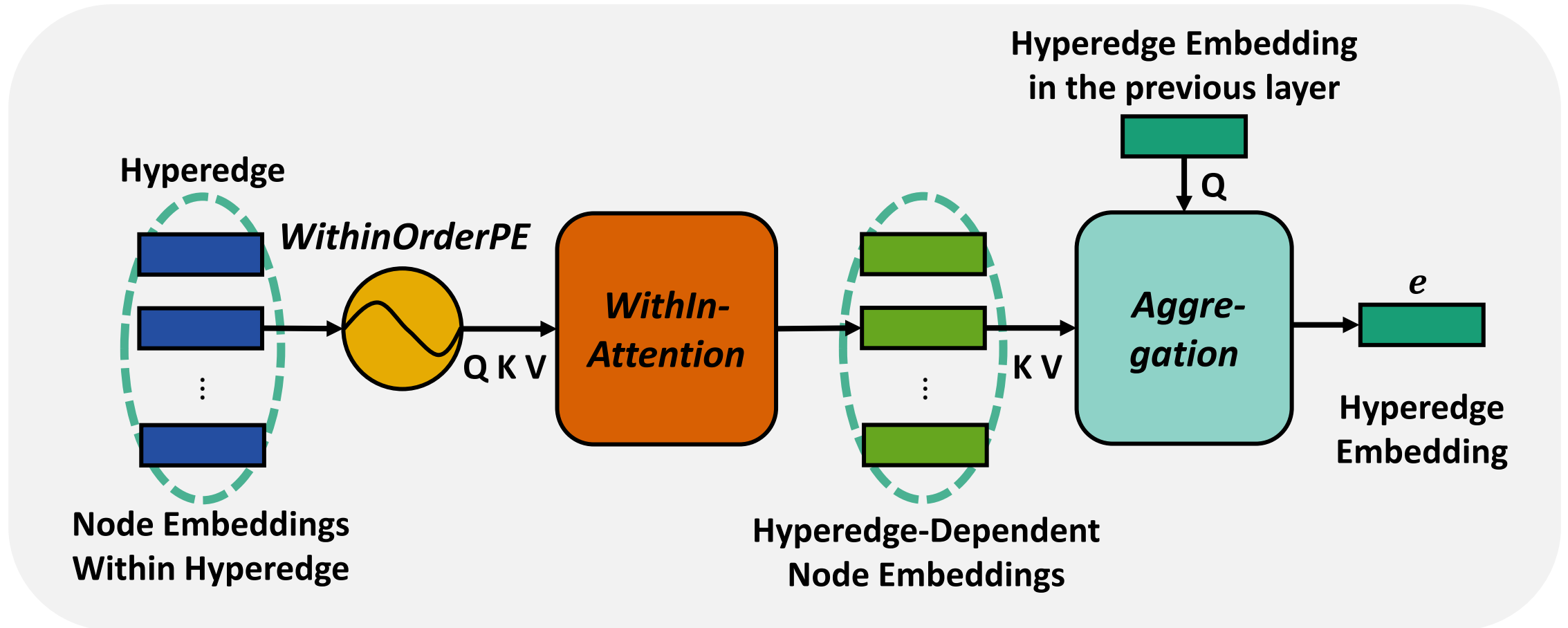
Labels: To, From, or Ccs

Roadmap

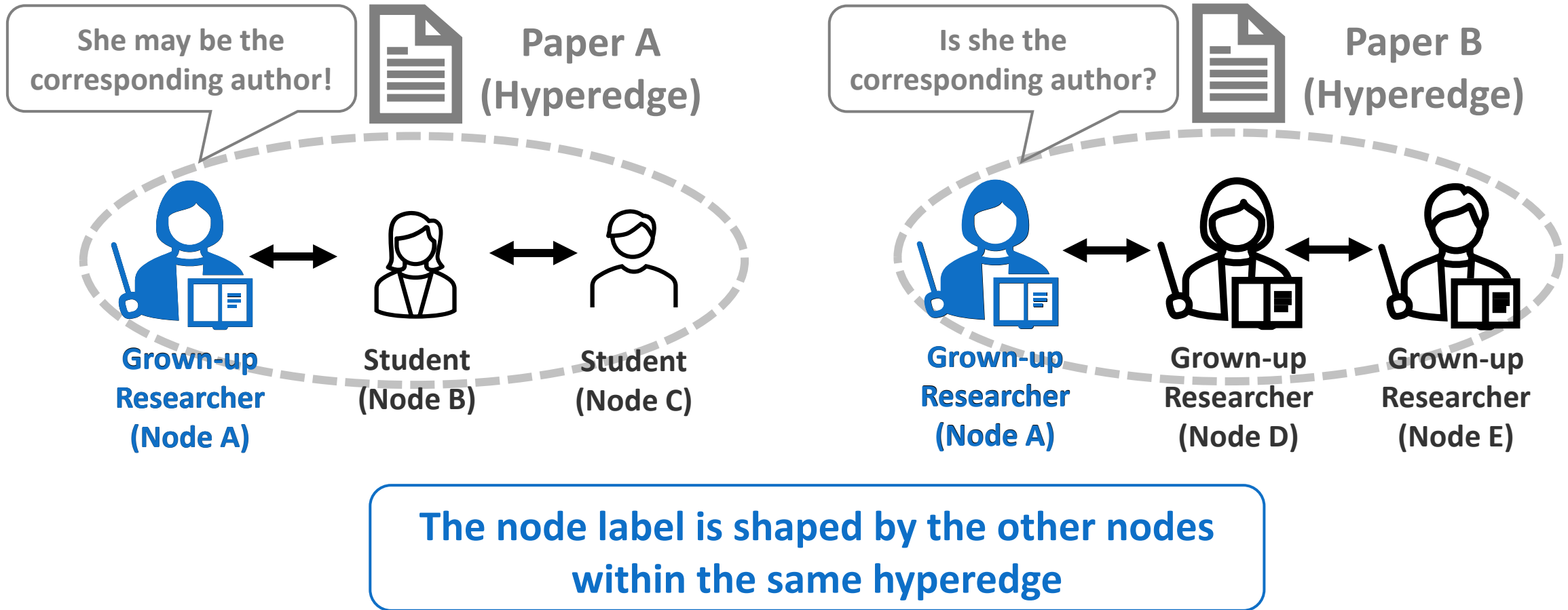
1. Introduction
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- 3. WHATsNET: Proposed Approach <<**
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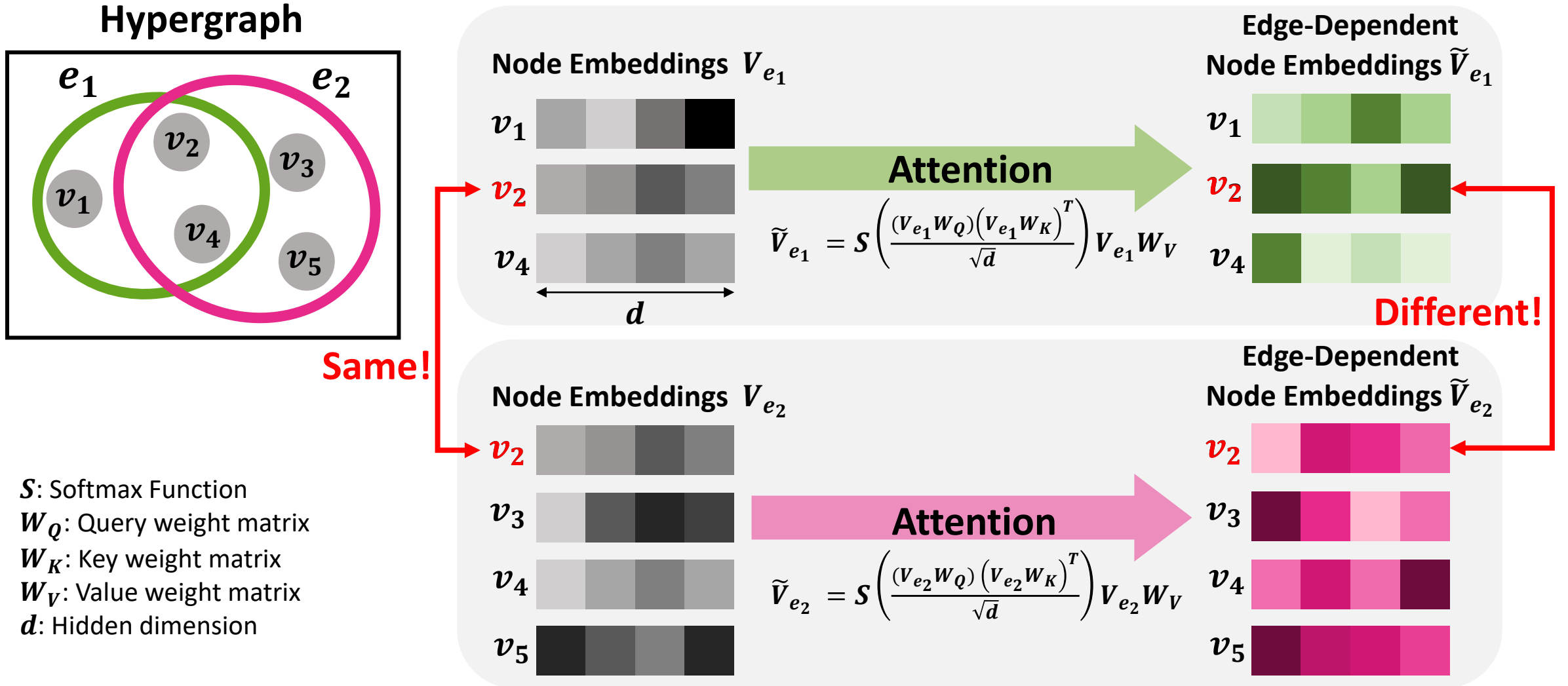
Proposed Model: WHATsNET



WithInATT: Attention to Other Nodes within Hyperedges

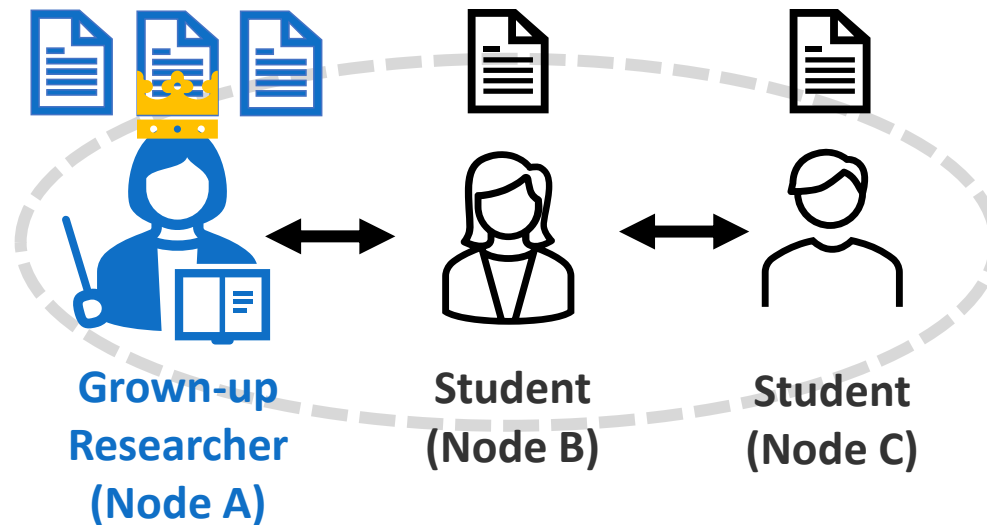


WithInATT: Attention to Other Nodes within Hyperedges



WithinOrderPE: Using Centrality for Positional Encoding

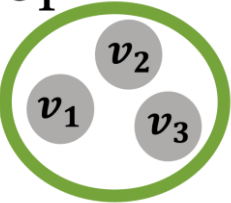
Papers = Degree Centrality

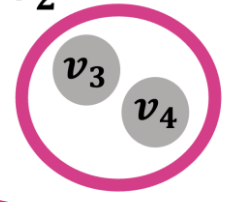


**The author with the highest centrality
is more likely to be the corresponding author!**

WithinOrderPE: Using Centrality for Positional Encoding

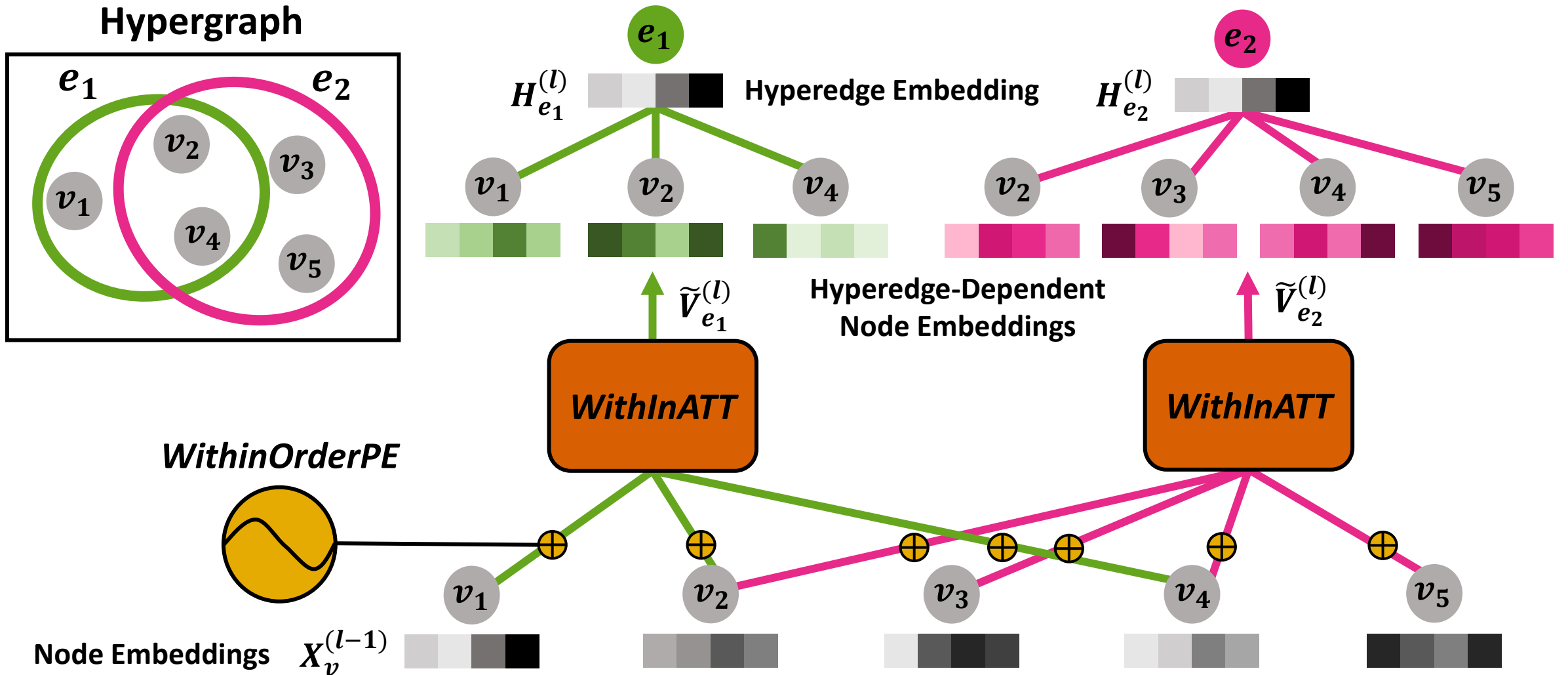
	Centrality Measure 1	Centrality Measure 2	Centrality Measure 3
Node v_1	3	0.7 3 th smallest	0.15
Node v_2	1	0.3 1 st smallest in e_1	0.15
Node v_3	3	0.5 2 nd smallest	0.15
Node v_4	2	0.5 same in e_2	0.2
\vdots	\vdots	\vdots	\vdots

e_1 	Within-OrderPE 1	Within-OrderPE 2	Within-OrderPE 3
Node v_1	2/3	3/(3 = $ e_1 $)	1/3
Node v_2	1/3	1/3	1/3
Node v_3	2/3	2/3	1/3

e_2 	Within-OrderPE 1	Within-OrderPE 2	Within-OrderPE 3
Node v_3	2/(2 = $ e_2 $)	1/2	1/2
Node v_4	1/2	1/2	2/2

Different!

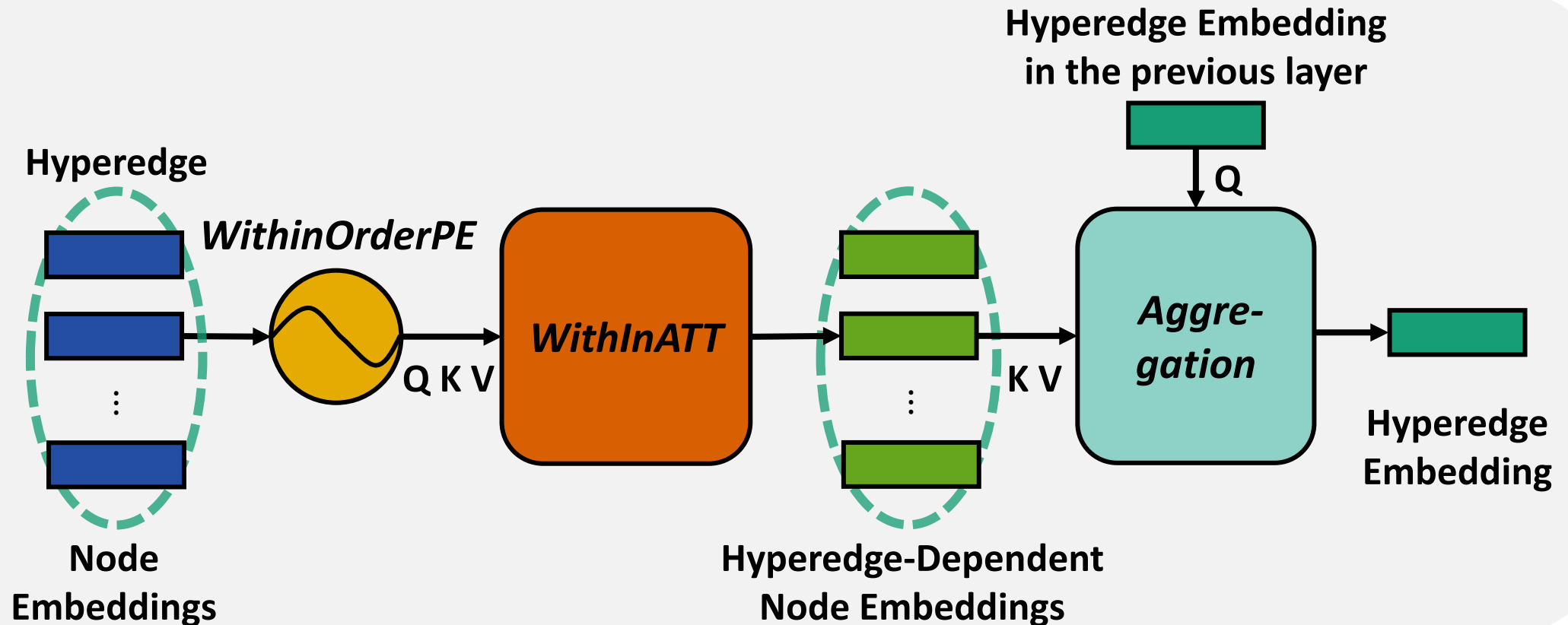
WHATsNET: Our Final Model



WHATsNET: Our Final Model

First Update Step) Node→Hyperedge:

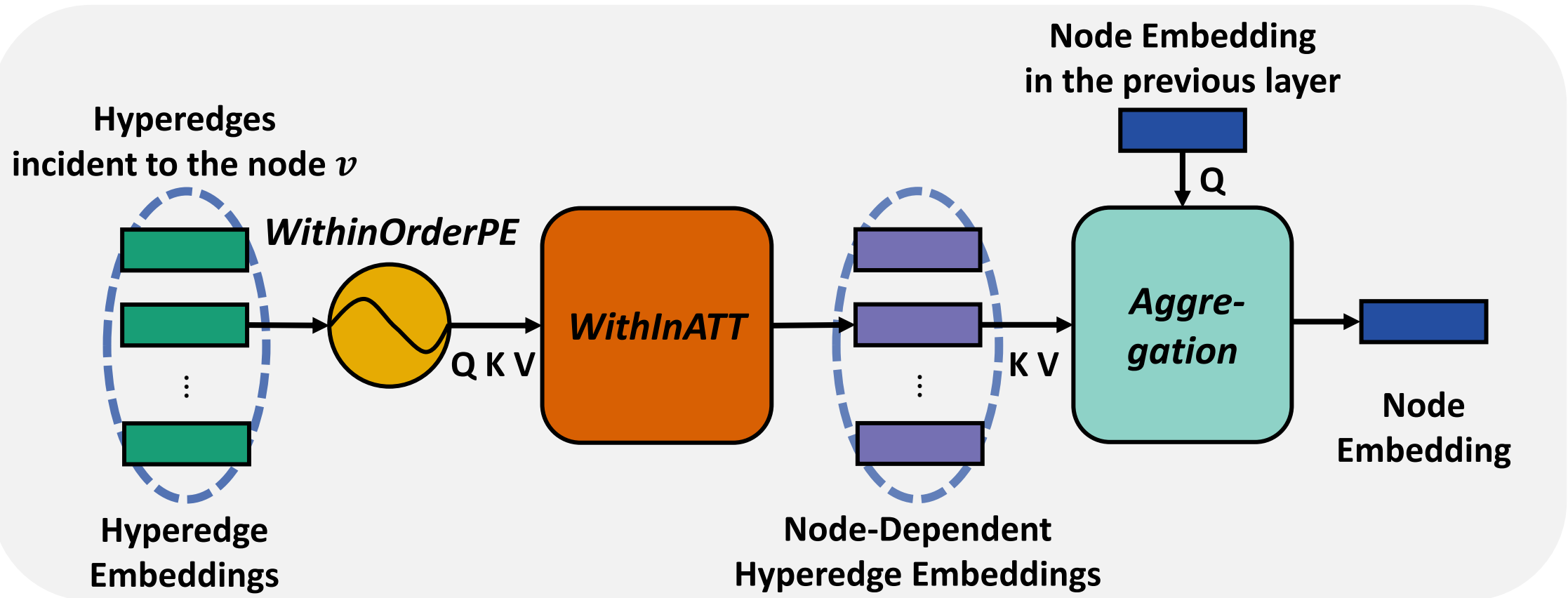
Update each hyperedge embedding using node embeddings within it



WHATsNET: Our Final Model

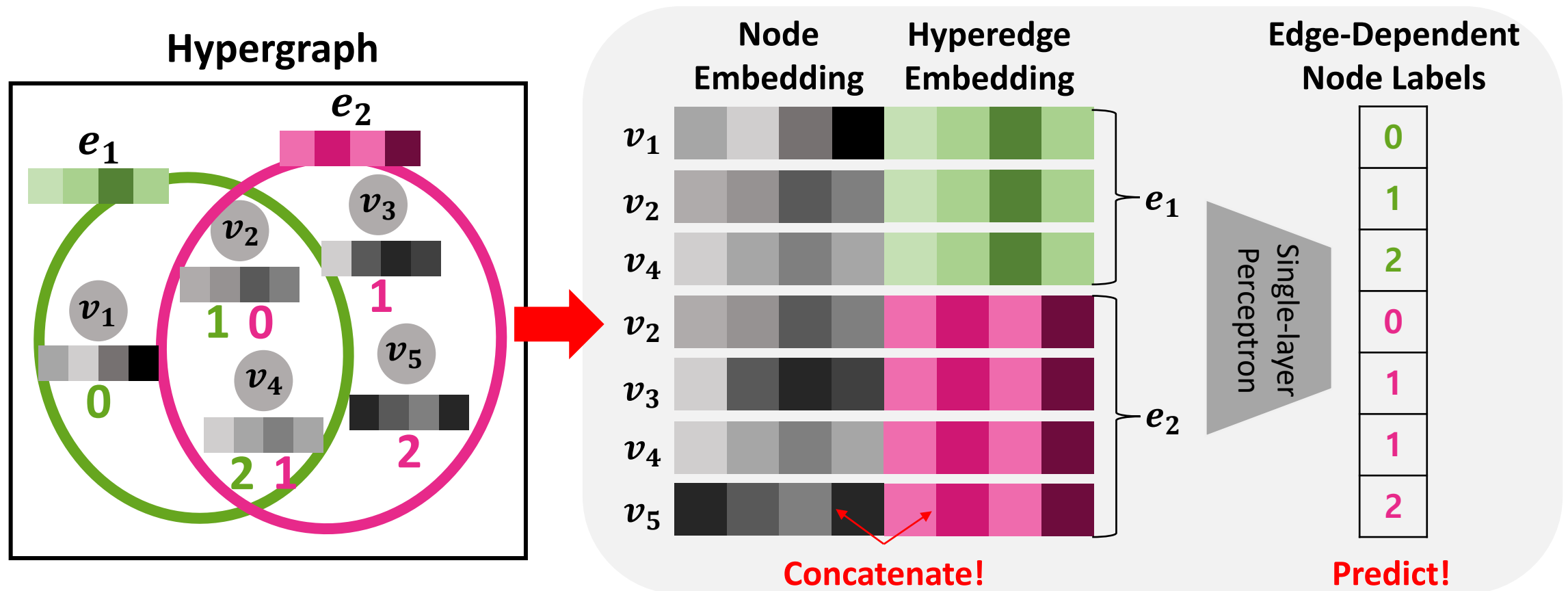
Second Update Step) Hyperedge \rightarrow Node:

Update each node embedding using hyperedge embeddings including it



WHATsNET: Our Final Model

Classifier) Edge-dependent node labels are predicted using the concatenation of node and hyperedge embeddings from the last layer of WHATsNET



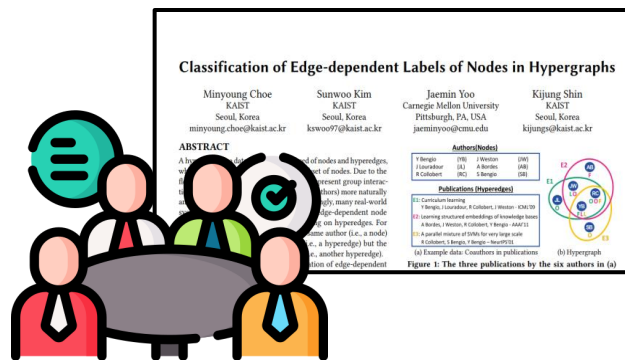
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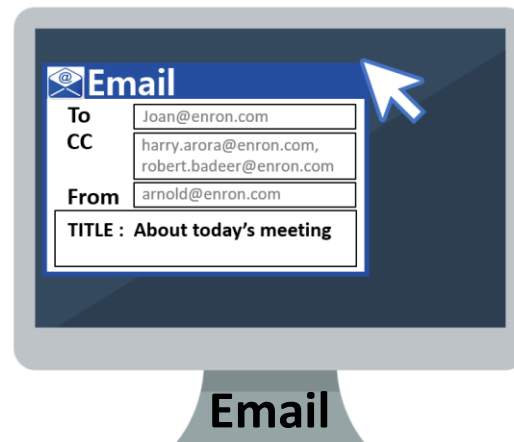


Experiment Setting

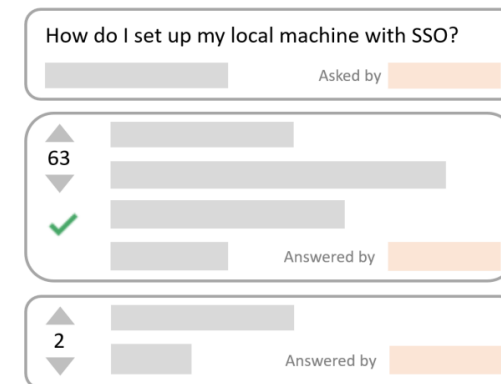
- **Six real-world datasets** from three domains
 - Co-Authorship, Email, and Online Q&A Platform
- **Eight baseline approaches** of hypergraph neural networks
 - HNHN, HGNN, HCHA, HAT, UniGCNII, HNN, HST, and AST
- **Three applications** where edge-dependent node labels are useful
 - Ranking Aggregation, Clustering, and Product Return Prediction



Co-Authorship



Email



Q&A Platform

Q1. Edge-Dependent Node Classification

Q1. Does *WHATsNet* accurately predict the edge-dependent labels of nodes?

A1. **WHATsNET consistently outperforms 10 competitors in classifying edge-dependent labels of nodes across all 6 datasets!**

Results of Edge-Dependent Node Classification

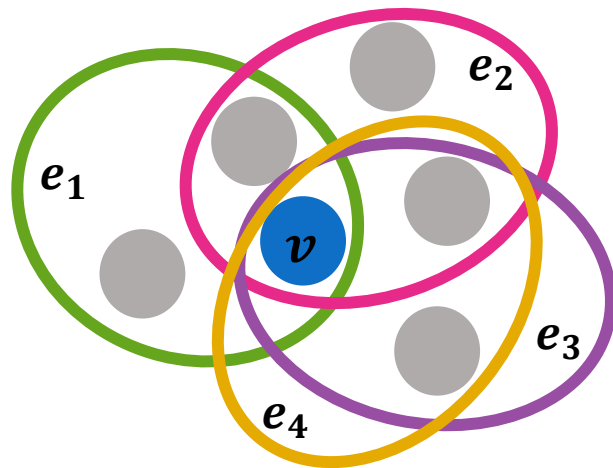
Dataset	Metric	BaselineU	BaselineP	HNHN	HGNN	HCHA	HAT	UniGCNII	HNN	HST	AST	WHATsNET
Coauth-DBLP	MicroF1	0.333 ± 0.001	0.346 ± 0.001	0.486 ± 0.004	0.540 ± 0.004	0.451 ± 0.007	0.503 ± 0.004	0.497 ± 0.003	0.488 ± 0.006	0.564 ± 0.004	0.495 ± 0.038	0.605 ± 0.002
	MacroF1	0.330 ± 0.001	0.332 ± 0.001	0.478 ± 0.008	0.519 ± 0.002	0.334 ± 0.048	0.483 ± 0.006	0.476 ± 0.002	0.482 ± 0.006	0.549 ± 0.003	0.487 ± 0.040	0.595 ± 0.002
Coauth-AMiner	MicroF1	0.334 ± 0.000	0.339 ± 0.000	0.520 ± 0.002	0.566 ± 0.002	0.468 ± 0.020	0.543 ± 0.002	0.520 ± 0.001	0.543 ± 0.002	0.596 ± 0.007	0.577 ± 0.005	0.630 ± 0.005
	MacroF1	0.332 ± 0.000	0.333 ± 0.000	0.514 ± 0.002	0.551 ± 0.004	0.447 ± 0.040	0.533 ± 0.003	0.507 ± 0.001	0.533 ± 0.002	0.583 ± 0.008	0.570 ± 0.002	0.623 ± 0.007
Email-Enron	MicroF1	0.334 ± 0.001	0.439 ± 0.001	0.738 ± 0.028	0.725 ± 0.004	0.666 ± 0.010	0.817 ± 0.001	0.734 ± 0.010	0.763 ± 0.003	0.779 ± 0.067	0.796 ± 0.014	0.826 ± 0.001
	MacroF1	0.300 ± 0.001	0.333 ± 0.001	0.637 ± 0.023	0.674 ± 0.003	0.464 ± 0.002	0.753 ± 0.004	0.656 ± 0.010	0.679 ± 0.007	0.681 ± 0.123	0.719 ± 0.020	0.760 ± 0.004
Email-Eu	MicroF1	0.500 ± 0.001	0.525 ± 0.001	0.643 ± 0.004	0.633 ± 0.001	0.620 ± 0.000	0.669 ± 0.001	0.630 ± 0.005	OutOfMemory	0.671 ± 0.001	0.666 ± 0.005	0.671 ± 0.000
	MacroF1	0.493 ± 0.001	0.499 ± 0.001	0.552 ± 0.014	0.533 ± 0.008	0.497 ± 0.001	0.638 ± 0.002	0.565 ± 0.013	OutOfMemory	0.640 ± 0.002	0.624 ± 0.021	0.646 ± 0.003
Stack-Biology	MicroF1	0.335 ± 0.000	0.368 ± 0.001	0.640 ± 0.005	0.689 ± 0.002	0.589 ± 0.007	0.661 ± 0.005	0.610 ± 0.004	0.618 ± 0.015	0.694 ± 0.002	0.571 ± 0.054	0.742 ± 0.003
	MacroF1	0.326 ± 0.000	0.334 ± 0.003	0.592 ± 0.006	0.624 ± 0.007	0.465 ± 0.060	0.606 ± 0.005	0.433 ± 0.007	0.568 ± 0.013	0.631 ± 0.006	0.446 ± 0.081	0.686 ± 0.004
Stack-Physics	MicroF1	0.333 ± 0.001	0.370 ± 0.000	0.506 ± 0.053	0.686 ± 0.004	0.622 ± 0.003	0.708 ± 0.005	0.671 ± 0.022	0.683 ± 0.005	0.755 ± 0.010	0.728 ± 0.039	0.770 ± 0.003
	MacroF1	0.322 ± 0.001	0.332 ± 0.000	0.422 ± 0.043	0.630 ± 0.002	0.481 ± 0.007	0.643 ± 0.009	0.492 ± 0.016	0.617 ± 0.005	0.666 ± 0.013	0.646 ± 0.046	0.707 ± 0.004

Q2. Node Label Distribution Preservation

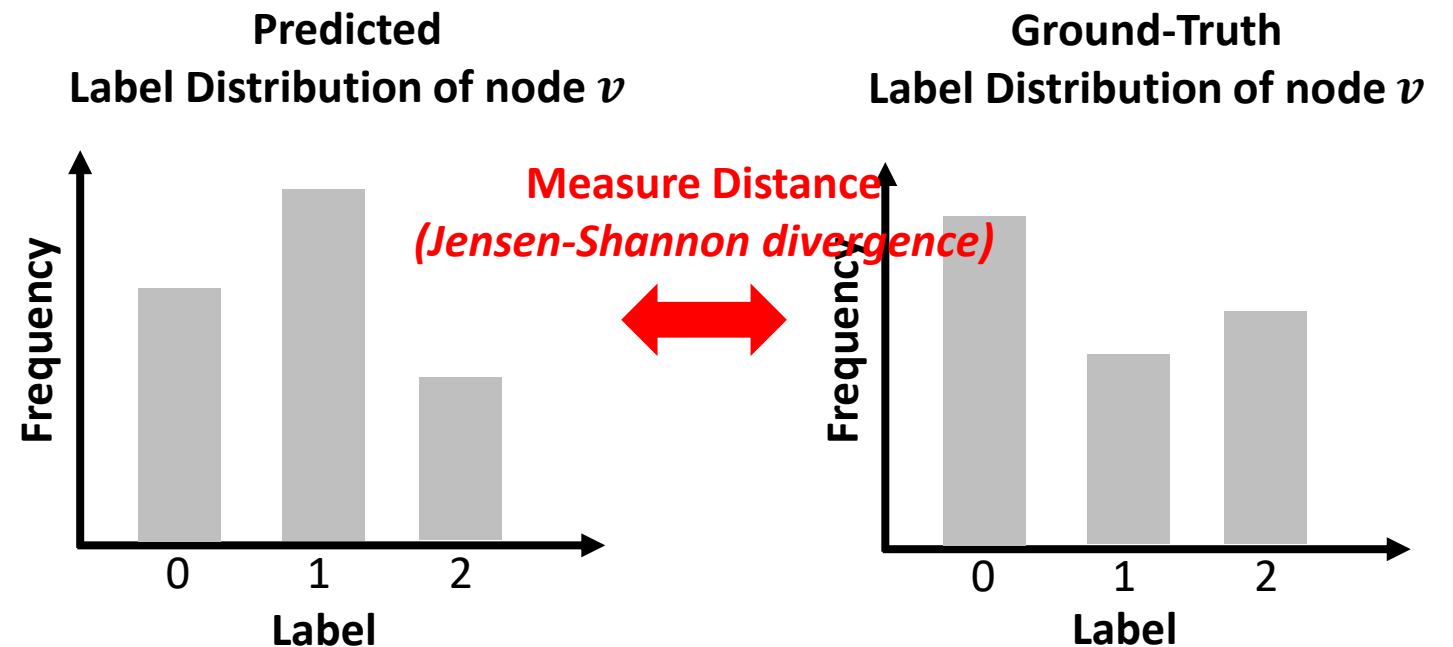
Q2. Does *WHATsNet* classify the same node differently depending on hyperedges?

To assess this, we examine *Node-Level Label Distribution*

= How many times each node has each label



	e_1	e_2	e_3	e_4
Label of v	0	1	2	1



Q2. Node Label Distribution Preservation

Q2. Does *WHATsNet* classify the same node differently depending on hyperedges?

A2. **WHATsNet preserves well** the ground-truth node-level label distributions

because it shows the smallest distance between ground-truth and predicted node label distribution

Jensen-Shannon divergence (JSD) between Ground-truth and Predicted Node Label Distributions

Dataset	BaselineU	BaselineP	HNHN	HGNN	HCHA	HAT	UniGCNII	HNN	HST	AST	WHATsNet
Coauth-DBLP	0.532 ± 0.002	0.518 ± 0.002	0.450 ± 0.002	0.394 ± 0.005	0.450 ± 0.002	0.429 ± 0.004	0.449 ± 0.006	0.450 ± 0.003	0.388 ± 0.006	0.453 ± 0.038	0.350 ± 0.002
Coauth-AMiner	0.529 ± 0.000	0.523 ± 0.000	0.440 ± 0.003	0.372 ± 0.002	0.462 ± 0.002	0.414 ± 0.003	0.424 ± 0.002	0.411 ± 0.003	0.356 ± 0.005	0.382 ± 0.009	0.328 ± 0.004
Email-Enron	0.486 ± 0.002	0.395 ± 0.001	0.162 ± 0.003	0.212 ± 0.007	0.291 ± 0.007	0.157 ± 0.004	0.187 ± 0.002	0.205 ± 0.002	0.302 ± 0.233	0.178 ± 0.019	0.136 ± 0.001
Email-Eu	0.199 ± 0.006	0.164 ± 0.004	0.232 ± 0.009	0.291 ± 0.001	0.268 ± 0.002	0.154 ± 0.004	0.300 ± 0.004	OutOfMemory	0.158 ± 0.005	0.168 ± 0.015	0.151 ± 0.009
Stack-Biology	0.536 ± 0.001	0.467 ± 0.003	0.266 ± 0.007	0.202 ± 0.003	0.237 ± 0.016	0.235 ± 0.006	0.263 ± 0.004	0.311 ± 0.026	0.200 ± 0.002	0.259 ± 0.022	0.152 ± 0.002
Stack-Physics	0.532 ± 0.001	0.482 ± 0.001	0.286 ± 0.036	0.219 ± 0.008	0.289 ± 0.004	0.227 ± 0.006	0.285 ± 0.050	0.292 ± 0.005	0.162 ± 0.008	0.185 ± 0.021	0.141 ± 0.003

Q3. Ablation Study of WHATsNet

Q3. Does each component make a meaningful contribution to the performance?

A3-(a). Importance of WithinATT

WHATsNet consistently outperforms the variant without WithinATT.

A3-(b). Improvement by WithinOrderPE

WHATsNet also performs better than the variant without WithinOrderPE

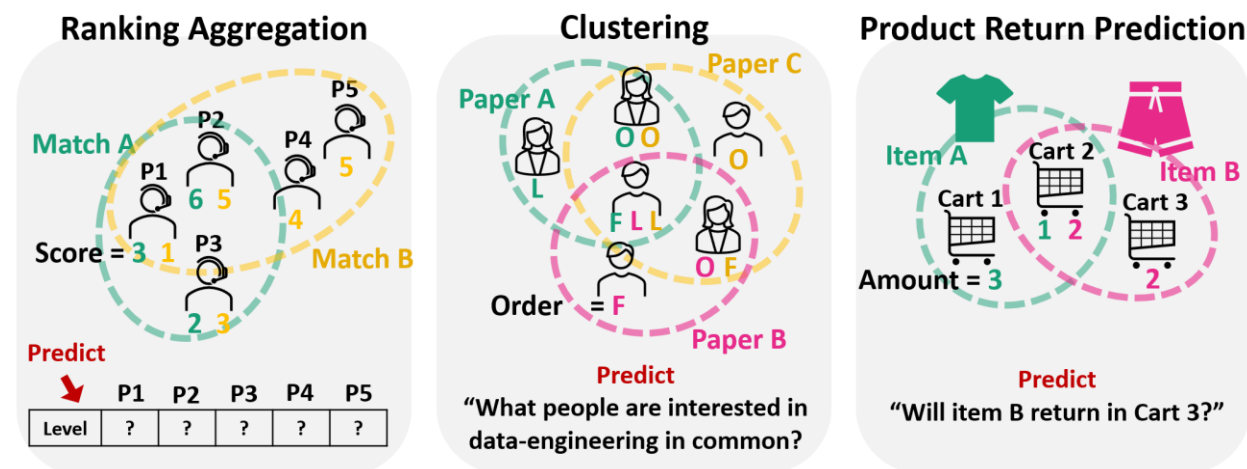
Dataset	Metric	w/o WITHINATT	w/o WITHINORDERPE	WHATsNET
Coauth-DBLP	MicroF1	0.581 ± 0.004	0.591 ± 0.003	0.605 ± 0.002
	MacroF1	0.577 ± 0.003	0.584 ± 0.003	0.595 ± 0.002
Coauth-AMiner	MicroF1	0.604 ± 0.010	0.583 ± 0.095	0.630 ± 0.005
	MacroF1	0.592 ± 0.013	0.536 ± 0.174	0.623 ± 0.007
Email-Enron	MicroF1	0.812 ± 0.008	0.825 ± 0.001	0.826 ± 0.001
	MacroF1	0.747 ± 0.014	0.762 ± 0.004	0.760 ± 0.004
Email-Eu	MicroF1	0.651 ± 0.019	0.670 ± 0.000	0.671 ± 0.000
	MacroF1	0.630 ± 0.018	0.638 ± 0.002	0.646 ± 0.003
Stack-Biology	MicroF1	0.723 ± 0.002	0.732 ± 0.002	0.742 ± 0.003
	MacroF1	0.656 ± 0.005	0.672 ± 0.004	0.686 ± 0.004
Stack-Physics	MicroF1	0.752 ± 0.005	0.765 ± 0.002	0.770 ± 0.003
	MacroF1	0.675 ± 0.010	0.688 ± 0.008	0.707 ± 0.004
AVG. Ranking	MicroF1	2.83	2.17	1.00
	MacroF1	2.83	2.00	1.17

Q4. Usefulness in Downstream Tasks

Q4. How can we apply *WHATsNet* to real-world downstream tasks?

Does WHATsNet show usefulness in these tasks?

A4. In *three* downstream tasks, we compare the performance of the tasks using
(a) ground-truth edge-dependent node labels, (b) labels predicted by WHATs-
NET, (c) No labels

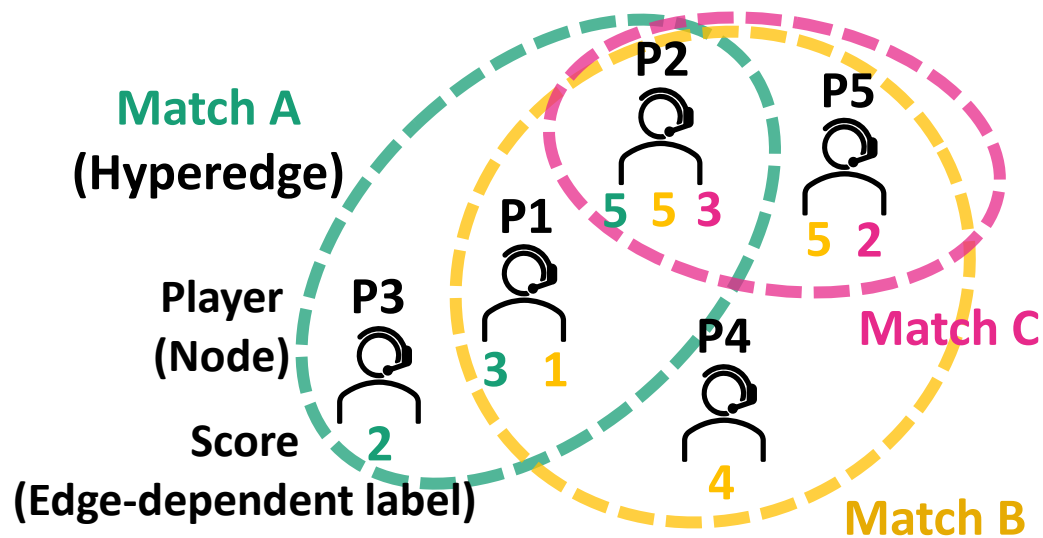


Q4. Usefulness in Downstream Tasks

Q4. How can we apply *WHATsNet* to real-world downstream tasks?

Does WHATsNet show usefulness in these tasks?

A4. Ranking Aggregation Task:



	P1	P2	P3	P4	P5
Match A	3	2	5		
Match B	1	5		4	5
Match C		3			2

Given edge-dependent labels by (a), (b), or (c)

TASK: Predict!

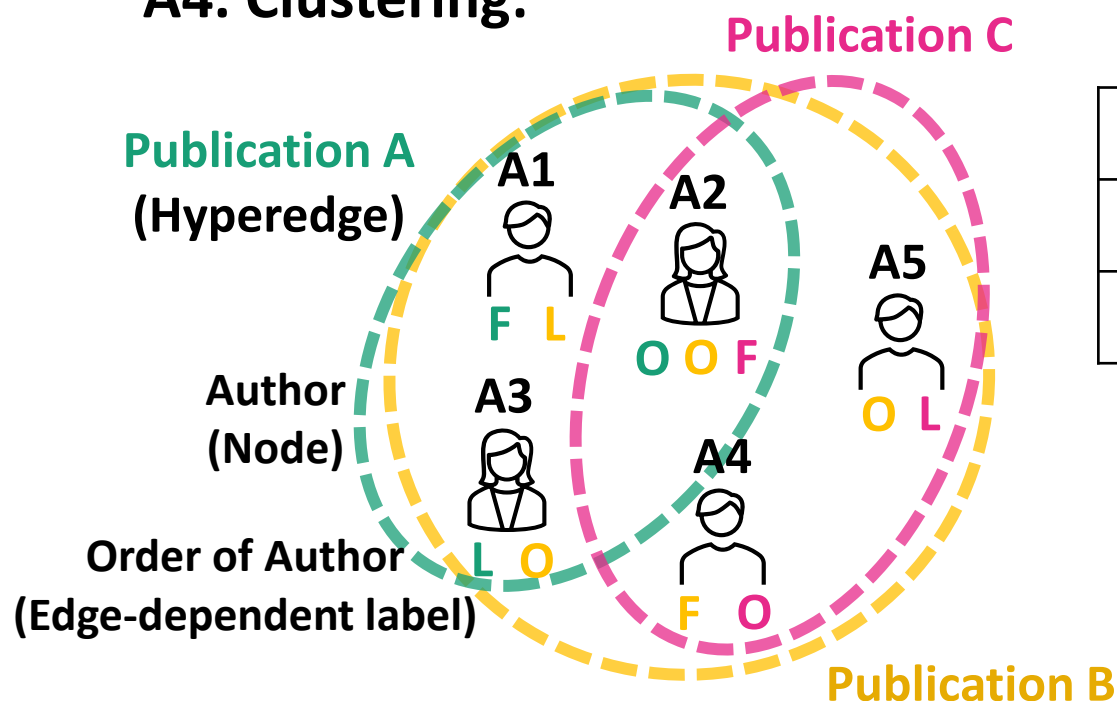
	P1	P2	P3	P4	P5
Level	?	?	?	?	?

Q4. Usefulness in Downstream Tasks

Q4. How can we apply *WHATsNet* to real-world downstream tasks?

Does WHATsNet show usefulness in these tasks?

A4. Clustering:



	A1	A2	A3	A4	A5
Publication A	F	O	L		
Publication B	L	O	O	F	O
Publication C		F		O	L

Given
edge-dependent
labels by
(a), (b), or (c)



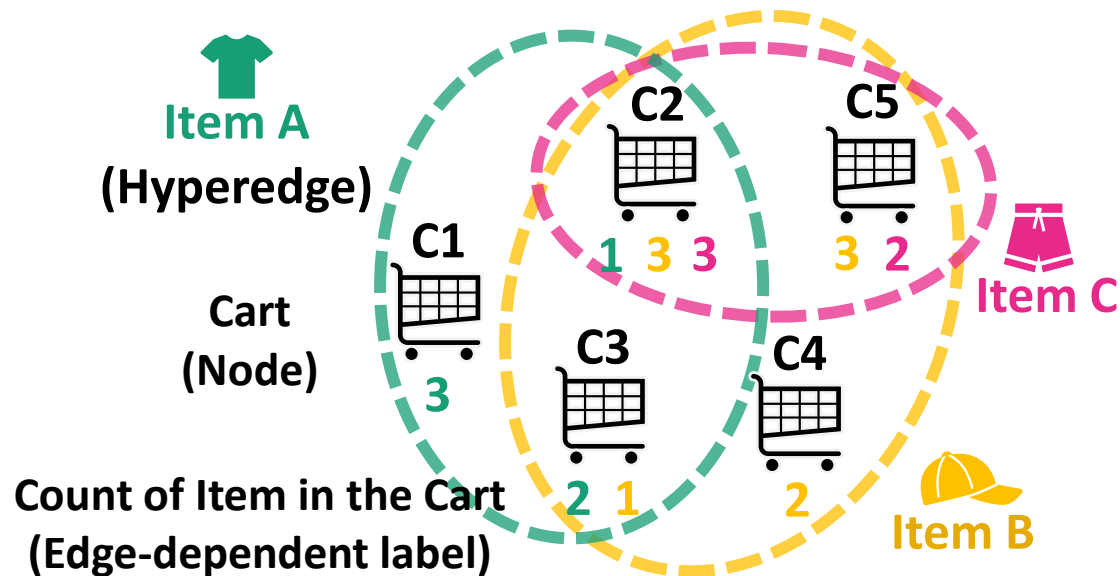
TASK: Cluster publications with the same venue!

Q4. Usefulness in Downstream Tasks

Q4. How can we apply *WHATsNet* to real-world downstream tasks?

Does WHATsNet show usefulness in these tasks?

A4. Product Return Prediction:



	C1	C2	C3	C4	C5
Item A	3	1	2		
Item B	1	3	1	2	3
Item C		3			2

Given edge-dependent labels by (a), (b), or (c)

TASK: Predict the likelihood of products being returned for each cart!

Q4. Usefulness in Downstream Tasks

Q4. How can we apply WHATsNet to real-world downstream tasks?

Does WHATsNet show usefulness in these tasks?

A4. Utilization of edge-dependent node labels predicted by **WHATsNet** *consistently leads to performance improvements* compared to the results obtained *without labels*.

(a) Ranking Aggregation (Accuracy)

Method	Halo	H-Index
RW [13] w/ Ground Truth	<u>0.711</u>	0.675
RW [13] w/ WHATsNET	0.714	0.693
RW [13] w/ HST	0.707	<u>0.695</u>
RW [13] w/ AST	0.706	0.696
RW [13] w/o Labels	0.532	0.654

(b) Clustering (NMI: The higher, the better)

Method	DBLP	AMiner
RDC-Spec [23] w/ GroundTruth	0.221	0.359
RDC-Spec [23] w/ WHATsNET	<u>0.184</u>	<u>0.352</u>
RDC-Spec [23] w/ HST	0.166	0.339
RDC-Spec [23] w/ AST	0.168	0.332
RDC-Spec [23] w/o Labels	0.163	0.338

(c) Product Return Prediction (F1)

Method	Synthetic E-tail
HyperGO [38] w/ GroundTruth	0.738
HyperGO [38] w/ WHATsNET	0.723
HyperGO [38] w/ HST	<u>0.724</u>
HyperGO [38] w/ AST	0.721
HyperGO [38] w/o Labels	0.718

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Conclusion

- Our contributions are summarized as follows:

- ✓ **New Problem:** Formulate the edge-dependent node classification problem
- ✓ **Effective Model:** Propose WHATsNET with WithInATT and WithinOrderPE
- ✓ **Extensive Experiment:** Show the superiority of WHATsNET over 10 competitors



Code & Dataset: <https://github.com/young917/EdgeDependentNodeLabel>

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Jaemin Yoo: jaeminyoo@cmu.edu

Kijung Shin: kijungs@kaist.ac.kr



Minyoung Choe



Sunwoo Kim



Jaemin Yoo



Kijung Shin

Appendix

Table 2: Summary of real-world hypergraphs with edge-dependent labels.

Dataset	Num. of Nodes	Num. of Hyperedges	Max. of Node Deg.	Max. of Hyperedge Size	Sum of Hyperedge Size	Num. of Class 0	Num. of Class 1	Num. of Class 2	Corr. w/ Centrality	Avg. Entropy
Coauth-DBLP	108,484	91,266	236	36	321,011	91,266	138,479	91,266	0.19	0.13
Coauth-AMiner	1,712,433	2,037,605	752	115	5,129,998	2,037,605	1,652,332	1,503,061	0.24	0.13
Email-Enron	21,251	101,124	18,168	948	1,186,521	635,268	450,129	101,124	0.10	0.28
Email-Eu	986	209,508	8,659	59	541,842	209,508	332,334	-	0.24	0.48
Stack-Biology	15,490	26,823	1,318	12	56,257	26,290	18,444	11,523	0.29	0.10
Stack-Physics	80,936	200,811	6,332	48	479,809	194,575	201,121	84,113	0.30	0.12

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Table 8: Comparison of positional encoding schemes. The symbol I_w denotes inducing points.

Dataset		w/o PE	Positional Encodings						WITHINORDERPE	
			GraphIT/DK	GraphIT/PRWK	Shaw/DK	Shaw/PRWK	LSPE	WholeOrderPE	w/o I_w	w/ I_w
Stack	MicroF1	0.732 ± 0.002	0.719 ± 0.006	0.710 ± 0.004	0.731 ± 0.003	0.456 ± 0.014	0.727 ± 0.003	0.732 ± 0.003	0.737 ± 0.006	0.737 ± 0.003
Biology	MacroF1	0.672 ± 0.004	0.645 ± 0.012	0.638 ± 0.012	0.667 ± 0.005	0.338 ± 0.038	0.658 ± 0.010	0.669 ± 0.011	0.680 ± 0.005	0.679 ± 0.007

Table 9: Comparison of node-centrality measures that can be used for WITHINORDERPE.

Dataset		Degree	Coreness	Eigenvector	PageRank	H-Coreness	H-Eigenvector	Vector Centrality	WHATsNET	WHATsNET-all
Stack	MicroF1	0.735 ± 0.001	0.739 ± 0.005	0.738 ± 0.003	0.741 ± 0.003	0.738 ± 0.005	0.738 ± 0.004	0.745 ± 0.002	0.742 ± 0.003	0.745 ± 0.002
Biology	MacroF1	0.678 ± 0.004	0.685 ± 0.010	0.681 ± 0.004	0.681 ± 0.004	0.683 ± 0.008	0.681 ± 0.006	0.687 ± 0.003	0.686 ± 0.004	0.690 ± 0.005

Table 10: Effect of the number of inducing points and comparison of architectures for hyperedge-to-node message passing.

Dataset		Number of Inducing Points			MSG. Passing from Hyperedge to Node				
		2	4	8	HNHN	HAT	WHATsNET + HNHN	WHATsNET + HAT	WHATsNET
Stack	MicroF1	0.740 ± 0.002	0.742 ± 0.003	0.742 ± 0.003	0.640 ± 0.005	0.661 ± 0.005	0.645 ± 0.023	0.670 ± 0.015	0.742 ± 0.003
Biology	MacroF1	0.682 ± 0.006	0.686 ± 0.004	0.688 ± 0.002	0.592 ± 0.006	0.606 ± 0.005	0.583 ± 0.029	0.618 ± 0.010	0.686 ± 0.004

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Table 11: Effect of inputs to the final classifier

Dataset	Metric	Best Competitor	WHATsNET-IM	WHATsNET
Coauth-DBLP	MicroF1	0.564 ± 0.004	0.602 ± 0.002	0.605 ± 0.002
	MacroF1	0.549 ± 0.003	0.592 ± 0.002	0.595 ± 0.002
Coauth-AMiner	MicroF1	0.596 ± 0.007	0.637 ± 0.003	0.630 ± 0.005
	MacroF1	0.583 ± 0.008	0.631 ± 0.003	0.623 ± 0.007
Email-Enron	MicroF1	0.779 ± 0.067	0.858 ± 0.001	0.826 ± 0.001
	MacroF1	0.681 ± 0.123	0.796 ± 0.004	0.760 ± 0.004
Email-Eu	MicroF1	0.671 ± 0.001	0.687 ± 0.004	0.671 ± 0.000
	MacroF1	0.640 ± 0.002	0.660 ± 0.009	0.646 ± 0.003
Stack-Biology	MicroF1	0.694 ± 0.002	0.736 ± 0.003	0.742 ± 0.003
	MacroF1	0.631 ± 0.006	0.679 ± 0.007	0.686 ± 0.004
Stack-Physics	MicroF1	0.755 ± 0.010	0.769 ± 0.001	0.770 ± 0.003
	MacroF1	0.666 ± 0.013	0.692 ± 0.011	0.707 ± 0.004